

Realizați un document word cu numele **FORMULE** în care să introduceți următoarele ecuații matematice.

Margini: Sus 2cm, Jos 1 cm, Dreapta 2 cm, Stânga 1.5 cm

Orientare: Portret,

Dimensiune: A4

Inscriptionare: Inserarea ecuațiilor

Bordură de pagină: 3D, culoare verde, lățime 3 pct

1)

$$\begin{aligned}\cos \frac{7\pi}{12} &= \cos \frac{3\pi + 4\pi}{12} = \cos \left(\frac{3\pi}{12} + \frac{4\pi}{12} \right) = \cos \left(\frac{\pi}{4} + \frac{\pi}{3} \right) = \\ &= \cos \frac{\pi}{4} \cos \frac{\pi}{3} - \sin \frac{\pi}{4} \sin \frac{\pi}{3} = \frac{\sqrt{2}}{2} \cdot \frac{1}{2} - \frac{\sqrt{2}}{2} \cdot \frac{\sqrt{3}}{2} = \frac{\sqrt{2}}{4} - \frac{\sqrt{6}}{4} = \frac{\sqrt{2} - \sqrt{6}}{4} \\ \sin \frac{7\pi}{12} &= \sin \left(\frac{3\pi + 4\pi}{12} \right) = \sin \left(\frac{3\pi}{12} + \frac{4\pi}{12} \right) = \sin \frac{\pi}{4} \cos \frac{\pi}{3} + \sin \frac{\pi}{3} \cos \frac{\pi}{4} = \\ &= \frac{\sqrt{2}}{2} \cdot \frac{1}{2} + \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{2}}{2} = \frac{\sqrt{2}}{4} + \frac{\sqrt{6}}{4} = \frac{\sqrt{2} + \sqrt{6}}{4}\end{aligned}$$

2) $(a + b)^2 = a^2 + 2ab + b^2$

$$\begin{aligned}(x + \sqrt{5})^2 &= x^2 + 2x\sqrt{5} + \sqrt{5}^2 = \\ &= x^2 + 2\sqrt{5}x + 5;\end{aligned}$$

$$\begin{aligned}(xy + 3\sqrt{5})^2 &= (xy)^2 + 2 \cdot xy \cdot 3\sqrt{5} + (3\sqrt{5})^2 \\ &= x^2y^2 + 6xy\sqrt{5} + 3^2\sqrt{5}^2 = \\ &= x^2y^2 + 6xy\sqrt{5} + 45;\end{aligned}$$

$(a - b)^2 = a^2 - 2ab + b^2$

$$\begin{aligned}(\sqrt{2} - y)^2 &= \sqrt{2}^2 - 2\sqrt{2}y + y^2 = \\ &= 4 - 2\sqrt{2}y + y^2;\end{aligned}$$

$$\begin{aligned}\left(xy - \frac{3}{2}\right)^2 &= x^2y^2 - 2xy \frac{3}{2} + \left(\frac{3}{2}\right)^2 = \\ &= x^2y^2 - 3xy + \frac{9}{4};\end{aligned}$$

3)

$$6x^4 + 5x^3 - 38x^2 + 5x + 6 = 0 \Leftrightarrow 6\left(x^2 + \frac{1}{x^2}\right) + 5\left(x + \frac{1}{x}\right) - 38 = 0 \Leftrightarrow$$

$$\Leftrightarrow 6\left[\left(x + \frac{1}{x}\right)^2 - 2\right] + 5\left(x + \frac{1}{x}\right) - 38 = 0 \Leftrightarrow \begin{cases} 6t^2 + 5t - 50 = 0, \\ t = x + \frac{1}{x}, \end{cases} \Leftrightarrow$$

$$\Leftrightarrow \begin{cases} \begin{cases} t_1 = -\frac{10}{3}, \\ t_2 = \frac{5}{2}, \\ t = x + \frac{1}{x}, \end{cases} \Leftrightarrow \begin{cases} x + \frac{1}{x} = -\frac{10}{3}, \\ x + \frac{1}{x} = \frac{5}{2}, \end{cases} \Leftrightarrow \begin{cases} 3x^2 + 10x + 3 = 0, \\ 2x^2 - 5x + 2 = 0, \end{cases} \Leftrightarrow \begin{cases} x_1 = -3, \\ x_2 = -\frac{1}{3}, \\ x_3 = \frac{1}{2}, \\ x_4 = 2. \end{cases}$$

4)

$$\begin{cases} a_{11}x_1 + a_{12}x_2 + a_{13}x_3 = b_1 \\ a_{21}x_1 + a_{22}x_2 + a_{23}x_3 = b_2 \\ a_{31}x_1 + a_{32}x_2 + a_{33}x_3 = b_3 \end{cases} \text{ care are } A = \begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix}, \text{ cu}$$

$\det A \neq 0$, este un sistem Cramer si se rezolva parcurgand aceleasi etape:

o $d = \det A$.

$$\text{o } d_{x_1} = \begin{vmatrix} b_1 & a_{12} & a_{13} \\ b_2 & a_{22} & a_{23} \\ b_3 & a_{32} & a_{33} \end{vmatrix}; d_{x_2} = \begin{vmatrix} a_{11} & b_1 & a_{13} \\ a_{21} & b_2 & a_{23} \\ a_{31} & b_3 & a_{33} \end{vmatrix}; d_{x_3} = \begin{vmatrix} a_{11} & a_{12} & b_1 \\ a_{21} & a_{22} & b_2 \\ a_{31} & a_{32} & b_3 \end{vmatrix}$$

$$\text{o } x_1 = \frac{d_{x_1}}{d}; x_2 = \frac{d_{x_2}}{d}; x_3 = \frac{d_{x_3}}{d}.$$